

1) $SCF \subset CF$:

$$G = (\Sigma, P, \omega) \rightarrow G' = (N, T, P', S)$$

$$m_L(abc) = ABC$$

For $a \in \Sigma$: $A \in N, a \in T$

For $a \rightarrow x \in P$: $A \rightarrow a \in P'$

$S \in N$: $S \rightarrow m_L(\omega) \in P'$

$\{a, aa\} \in CF$

$\notin SCF$

2) SCF \subset PCF:

$$G = (\Sigma, P, \cup) \rightsquigarrow G' = (\Sigma, P', \cup)$$

$$P' = P \cup \{a \rightarrow a \mid a \in \Sigma\}$$

$$\{a^{2^n} \mid n \geq 0\} \in \text{PCF} - \text{SCF}$$

$$a \rightarrow aa$$

$$a \xrightarrow{P} aa \xrightarrow{P} aaaa \xrightarrow{P} \dots$$

3, $\text{JSCF}^{-\varepsilon} \subset \text{JSCF}$:

$\{a, ab\} \in \text{JSCF} : \cup = ab, P = \{b \rightarrow \varepsilon\}$

$\underline{ab} \xrightarrow{i} \underline{a}$

$\{a, ab\} \notin \text{JSCF}^{-\varepsilon} : \cup = a, P = \{a \rightarrow ab, \dots\}$

$a \xrightarrow{j} ab \xrightarrow{j} \cancel{ab}$

$\text{SCF}^{-\varepsilon} \subset \text{SCF} \quad \xrightarrow{j} b-ab$

$P = \{a \rightarrow ab\}, \cup = a$

$\text{JPCF}^{-\varepsilon} \subset \text{JPCF} : \underline{a} \xrightarrow{jP} \underline{ab}$
 $\text{PCF}^{-\varepsilon} \subset \text{PCF} \quad \{aa, aab\}$

$$L_A = \{a^{2^n} b^{2^m} \mid n \geq 0\} \notin \text{JPCF}$$

Assume $L(G, \text{ip} \Rightarrow) = L_A \in \text{JPCF}$.

$$L = ab, a \rightarrow x, b \rightarrow y \in P$$

$$1) x = \varepsilon, y \in L(G) \quad \begin{cases} y = ab : L(G, \text{ip} \Rightarrow) = \{ab\} \\ y = \varepsilon / a / b : \varepsilon \in L(G, \text{ip} \Rightarrow) \end{cases}$$

$$|y| > |ab|:$$

$$2) y = \varepsilon, x \in L(G) \quad \begin{matrix} ab \text{ ip} \Rightarrow \underline{aa} \underline{bb} \Rightarrow aabb \text{ } \times \\ \text{...} \end{matrix}$$

$$3) x \neq \varepsilon, y \neq \varepsilon:$$

$$3a) x = \underline{bx'} \text{ or } y = \underline{by'} : ab \text{ ip} \Rightarrow bz \times$$

$$3b) x = x'a \text{ or } y = y'a : ab \text{ ip} \Rightarrow za \times$$

$$3c) x = ax'b \text{ or } y = ay'b : ab \text{ ip} \Rightarrow ax \underline{ba} y'b \times$$